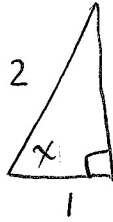


- +4 1. Find the exact value of $\arccos\left(\frac{1}{2}\right)$.

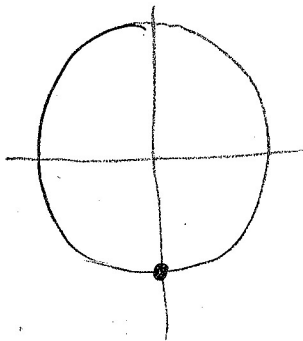
$$x = \arccos\left(\frac{1}{2}\right)$$



$30^\circ - 60^\circ - 90^\circ$
triangle

$$x = 60^\circ = \frac{\pi}{3}$$

- +4 2. Find the exact value of $\arcsin(-1)$.



Range of \arcsin : $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$

$$\arcsin(-1) = -\frac{\pi}{2}$$

- +4 3. Differentiate $y = \sqrt{\arctan(x)}$.

$$y = (\arctan(x))^{\frac{1}{2}}$$

$$f(x) = x^{\frac{1}{2}}$$

$$g(x) = \arctan(x)$$

$$f'(x) = \frac{1}{2} x^{-\frac{1}{2}}$$

$$g'(x) = \frac{1}{1+x^2}$$

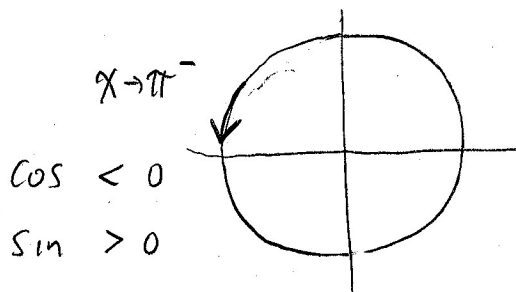
$$y' = f'(g(x)) g'(x)$$

$$= \frac{1}{2\sqrt{\arctan(x)}} \cdot \frac{1}{1+x^2}$$

$$= \frac{1}{2(1+x^2)\sqrt{\arctan(x)}}$$

4. Find $\lim_{x \rightarrow \pi^-} \frac{\sin(x)}{1 + \cos(x)}$. $\frac{0}{1+(-1)} = \frac{0}{0}$ use LR

$\stackrel{\text{LR}}{=} \lim_{x \rightarrow \pi^-} \frac{\cos(x)}{-\sin(x)} = \frac{-1}{0}$ So the limit DNE



$\frac{-}{-(+)} = +$, so the limit is DNE ($+\infty$)

5. Find $\lim_{x \rightarrow 0} \frac{1+x^2}{x}$. $\frac{1}{0}$

So, the limit DNE.

6. Find $\lim_{x \rightarrow 0} \frac{e^{2x} - 1 - 2x}{2x^2}$. $\frac{e^0 - 1 - 0}{0} = \frac{0}{0}$ use LR

$\stackrel{\text{LR}}{=} \lim_{x \rightarrow 0} \frac{2e^{2x} - 2}{4x} = \lim_{x \rightarrow 0} \frac{2(e^{2x} - 1)}{4x} = \lim_{x \rightarrow 0} \frac{e^{2x} - 1}{2x} = \frac{1-1}{0} = \frac{0}{0}$

$\stackrel{\text{LR}}{=} \lim_{x \rightarrow 0} \frac{2e^{2x}}{2} = \lim_{x \rightarrow 0} e^{2x} = 1$

use LR