

1. Consider the sets $A = \{2, 3, 5\}$ and $B = \{3, 8\}$, and the relation $(x, y) \in R \iff x^2 + y^2$ is odd. Compute the inverse relation R^{-1} , as well as the matrix representation for R^{-1} .

2. Consider the sets $A = \{a_1, a_2, a_3\}$, $B = \{b_1, b_2\}$, and $C = \{c_1, c_2, c_3\}$, with the following relations from R from A to B , and S from B to C :

$$R = \{(a_1, b_2), (a_2, b_1), (a_3, b_1)\},$$

$$S = \{(b_1, c_2), (b_1, c_3), (b_2, c_1)\}.$$

What is the matrix of $R \circ S$?

3. The relation \leq on \mathbb{Z} is (circle all that apply):

- (a) reflexive,
- (b) symmetric,
- (c) antisymmetric,
- (d) transitive,
- (e) a partial order,
- (f) an equivalence relation.

4. Consider the relation R on \mathbb{N} given by $m \sim n$ when m and n have *exactly* the same digits, but perhaps in a different order. Thus, $1233 \sim 3213$, but $1233 \not\sim 321$. The relation \sim on \mathbb{N} is (circle all that apply):
- (a) reflexive,
 - (b) symmetric,
 - (c) antisymmetric,
 - (d) transitive,
 - (e) a partial order,
 - (f) an equivalence relation.
5. Let A be the set of all subsets of $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$. Is the subset relation \subseteq on A a partial order? Justify your answer.
6. Let \models be a relation on \mathbb{N} such that $m \models n$ if m and n both begin with the same digit. Thus, $123 \models 1973$, but *not* $123 \models 213$. Is the relation \models on \mathbb{N} an equivalence relation? Justify your answer.